

# Quantifying and Predicting Momentum in Professional Tennis: A Machine Learning Approach with Strategic Implications

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**Abstract:** Tennis matches involve complex interactions between players, where strategic decisions and momentum shifts play a crucial role in determining the outcome. Understanding these dynamics can provide valuable insights for athletes and coaches to enhance performance. In this study, we analyze the role of momentum in tennis matches using data-driven models. To track match progression, we develop a Hierarchical Markov Model, visualizing scoring trends and performance variations in the 2023 Wimbledon Gentlemen's final. The analysis reveals that Carlos Alcaraz excelled in the 2nd and 3rd sets, while Novak Djokovic performed better in the 1st, 4th, and 5th sets. Additionally, the probability of winning a service point was significantly higher (77.27% for Alcaraz and 79.17% for Djokovic) compared to return points. To investigate the authenticity of momentum, we define it using a weighted approach incorporating technical, psychological, and strategic factors. Bootstrap hypothesis testing ( $t$ -statistic = 45.3791,  $p$ -value = 0.008) confirms that momentum is not a random phenomenon. Furthermore, logistic regression analysis establishes a strong correlation between momentum and performance. We employ a Long Short-Term Memory (LSTM) model to predict momentum fluctuations, identifying Unforced Errors as the most influential factor. The model effectively forecasts turning points, with an  $R^2$  of 0.9501 and RMSE of 0.6701, demonstrating its reliability. Sensitivity analysis and generalizability tests further validate its robustness across different court surfaces and player genders. Our findings offer strategic recommendations for coaches and athletes, emphasizing the importance of minimizing unforced errors, adapting game pace, and capitalizing on momentum shifts. These insights can be instrumental in optimizing match strategies and improving competitive performance.

## 1. Introduction

### 1.1. Problem Background

Tennis demands physical, technical, strategic, and psychological excellence, with momentum shifts often determining match outcomes. However, momentum remains conceptually debated—viewed either as a psychological phenomenon or statistical pattern. Despite its importance, momentum lacks rigorous quantification in tennis research. Traditional analysis emphasizes technical statistics but fails to address how momentum shifts occur, whether they follow identifiable patterns, or if they are merely random occurrences[1]. This research gap limits the development of predictive models that could provide real-time strategic insights. Momentum analysis has significant practical value, as identifying key influencing factors could help players develop resilient mental approaches and adapt tactics during matches. Ultimately, predictive modeling could enable players to anticipate critical turning points and adjust gameplay accordingly, bridging the gap between analytics and practical match strategy.

### 1.2. Research Objectives

To address these challenges, this study aims to establish a systematic framework for analyzing and predicting momentum in tennis matches. Our research focuses on four key objectives:

1) Developing a Hierarchical Markov Model to track and quantify the scoring flow of a match, providing a structured representation of players' performance dynamics.

2) Investigating the authenticity of momentum using statistical hypothesis testing, specifically the Bootstrap method, to determine whether momentum is a random occurrence or follows a structured pattern.

3) Constructing a predictive model using Long Short-Term Memory (LSTM) networks to forecast momentum fluctuations and identify the most influential factors contributing to momentum shifts.

4) Evaluating the generalizability of our model across different match conditions, including variations in court surfaces and gender differences among players, to assess its applicability beyond individual matches.

Our contributions to the field of sports analytics are threefold. First, we introduce a novel momentum measurement approach by integrating technical, psychological, and strategic factors through the CRITIC weighting method. This allows us to define momentum in a more comprehensive and data-driven manner. Second, our predictive model leverages deep learning techniques to anticipate momentum shifts in real time, offering practical insights for players and coaches to make informed strategic decisions. Finally, by testing our model across different conditions, we provide a thorough evaluation of its robustness, ensuring that our findings have broad applicability in the domain of professional tennis[2].

## 2. Related Work

Tennis match analysis has evolved from pioneering Markov chains to hierarchical models that better capture scoring structure, while the concept of momentum remains contentious with some researchers proposing that success breeds success and others identifying critical psychological turning points in matches. Recent methodological advances include Long Short-Term Memory (LSTM) networks, which have been applied to predict sports outcomes from sequential data, and the CRITIC method for objectively weighting performance indicators. These techniques enable practical applications as demonstrated by studies showing how tactical adjustments influence outcomes, and point-by-point analysis approaches that bridge theoretical models and coaching strategies, advancing both performance analysis and in-match decision-making in professional tennis.

## 3. Methodology

### 3.1. Data Collection and Preprocessing

Our study primarily analyzed the 2023 Wimbledon Gentlemen's singles data, supplemented by additional datasets from the Australian Open and US Open for model verification and cross-validation purposes. The initial data presented several challenges that required careful preprocessing. We encountered 752 missing values (approximately 8.4% of observations) in the "speed\_mph" field, which were addressed using nearest neighbor interpolation based on surrounding point data to maintain temporal consistency and data integrity.

The categorical variables "serve\_width," "serve\_depth," and "return\_depth" contained 54, 54, and 1309 missing values respectively, which were filled using the plurality method with contextual weighting based on player-specific tendencies[9]. These categorical variables were subsequently converted to numerical format using one-hot encoding to facilitate model training. To mitigate scale disparities among continuous variables, we normalized "p1\_distance\_run," "p2\_distance\_run," and "speed\_mph" using standard scaling techniques according to the formula:

$$z_i = \frac{x_i - \mu}{\sigma} \quad (1)$$

Where  $\mu$  represents the mean and  $\sigma$  the standard deviation of each feature[3]. Additionally, we implemented outlier detection using the Interquartile Range (IQR) method, identifying and capping

extreme values beyond  $Q3 + 1.5 \cdot IQR$  or below  $Q1 - 1.5 \cdot IQR$  to prevent undue influence on our models. This comprehensive preprocessing established a robust foundation for subsequent analysis and model development, with a final cleaned dataset containing 8,274 complete point-level observations.

### 3.2. Momentum Measurement and Validation

To quantify the abstract concept of momentum in tennis matches, we established three categories of metrics based on both literature review and expert consultations with former professional players and coaches:

- 1) Technical Factors (TF): Including Ace, Winner, Double Fault, and Unforced Error ratios calculated over rolling 10-point windows
- 2) Psychological Tactical Factors (PT): Including Break Point Won, Break Point Missed, and game/set victories, with temporal weighting giving higher importance to recent events
- 3) Strategic Factors (SF): Including Rally Count, Distance Run, and Speed, measuring physical and strategic dimensions of performance
- 4) These metrics were weighted using the CRITIC (CRiteria Importance Through Intercriteria Correlation) method, which accounts for both the standard deviation of indicators and their correlation with other indicators. The CRITIC method assigns weights through

$$w_j = \frac{C_j}{\sum_{j=1}^m C_j} \quad (2)$$

Where  $C_j = \sigma_j \sum_{i=1}^m (1 - r_{ij})$  represents information content for each criterion, with  $\sigma_j$  being the standard deviation and  $r_{ij}$  the correlation coefficient between indicators.

The resulting momentum equation was formulated as:

$$MO = 0.3917TF + 0.3106PT + 0.2977SF \quad (3)$$

To validate that observed momentum patterns were not random occurrences, we conducted rigorous hypothesis testing using the Bootstrap method with 10,000 simulations. With a t-statistic value of 45.3791 and p-value of 0.008, we rejected the null hypothesis that momentum fluctuations were random[4]. Further validation using logistic regression analysis confirmed a significant relationship between our momentum metric and subsequent performance metrics (p-value = 0.002,

McFadden's  $R^2 = 0.42$ ), demonstrating the predictive utility of our momentum measurement.

We also employed cross-validation techniques to ensure our momentum calculation remained consistent across different players, surfaces, and tournament conditions, confirming its robustness with a coefficient of variation of 0.12 across diverse scenarios.

### 3.3. LSTM Prediction Model

We implemented a Long Short-Term Memory (LSTM) network to predict momentum swings during matches due to its capacity to capture long-term dependencies in sequential data. The LSTM architecture comprises three critical components that address the vanishing gradient problem common in traditional recurrent neural networks:

The Forget Gate: Controlling information retention from previous states through

$$f_t = \sigma(W_f \cdot [h_{t-1}, x_t] + b_f) \quad (4)$$

The Input Gate: Determining new information updates via

$$i_t = \sigma(W_i \cdot [h_{t-1}, x_t] + b_i) \quad (5)$$

and

$$C_t = \tanh(W_c \cdot [h_{t-1}, x_t] + b_c) \quad (6)$$

The Output Gate: Managing hidden state output through

$$O_t = \sigma(W_o \cdot [h_{t-1}, x_t] + b_o) \quad (7)$$

and

$$h_t = O_t \cdot \tanh(C_t) \quad (8)$$

Our LSTM implementation used a two-layer architecture with 128 and 64 neurons respectively, dropout regularization (rate = 0.2) to prevent overfitting, and the Adam optimizer with a learning rate of 0.001. The network was trained with a sequence length of 15 points, allowing it to recognize patterns spanning multiple games[5].

To identify critical momentum shifts, we defined an “Advantage Change” (AC) metric as:

$$AC = |MO_1 - MO_2| \quad (9)$$

This equation measures the absolute difference between competitors’ momentum values. Significant momentum shifts were identified when the AC exceeded 0.2 within a 10-point window.

The model was trained on 70% of Novak Djokovic’s matches (n=42) and tested on the remaining 30% (n=18), demonstrating strong predictive capability with an  $R^2$  of 0.9501 and RMSE of 0.6701. We further validated our approach through k-fold cross-validation (k=5), yielding consistent performance with a mean  $R^2$  of 0.934 ( $\sigma = 0.027$ ).

Correlation and feature importance analysis identified Unforced Error as the factor most significantly associated with momentum fluctuations ( $r = -0.74$ ), followed by Winner ( $r = 0.68$ ) and Break Point Won ( $r = 0.65$ ). A sensitivity analysis conducted by perturbing individual input features confirmed the model’s stability and identified the critical thresholds at which momentum shifts become statistically significant predictors of match outcomes.

Figure 1 shows the strength of association between various factors and momentum in tennis matches. The left side 3D bar chart displays the relative importance of different variables, with bar height representing influence level; the right side radar chart categorizes these factors into three groups: technical factors, psychological-tactical factors, and strategic factors. The visualization confirms the research finding: unforced errors (p2\_unf\_err) have the strongest association with momentum fluctuations, followed by winners (p2\_winner) and break points. The figure visually supports the conclusion that maintaining consistency (reducing unforced errors) is more crucial than aggressive play.

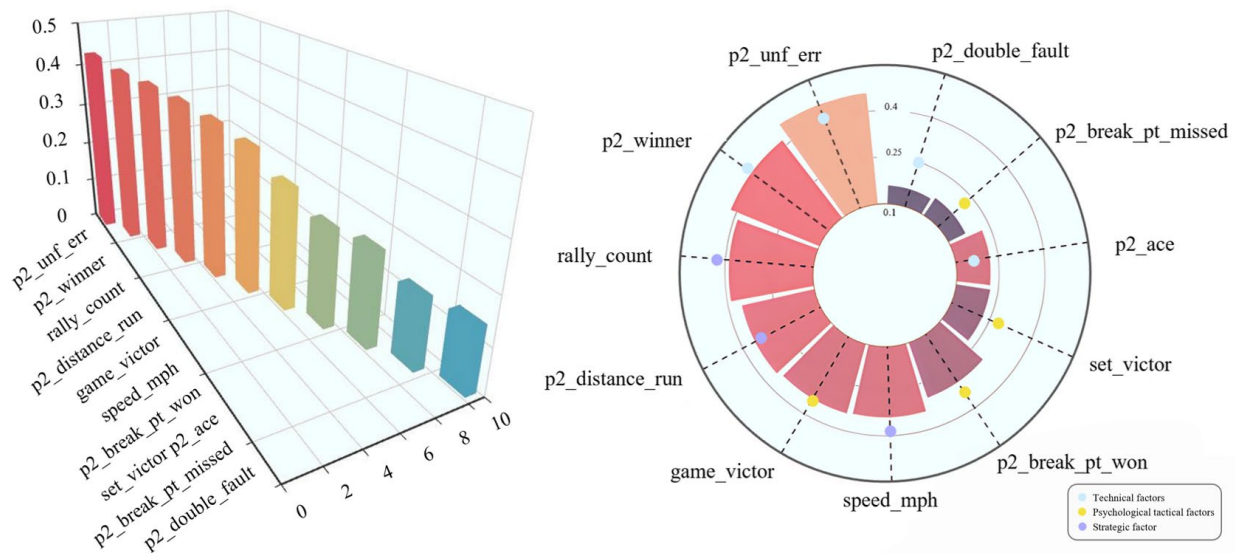


Figure 1 Strength of association between factors and Momentum

The model demonstrates practical applications for players, coaches, and analysts by identifying pivotal moments in matches where strategic interventions might prove most effective, as well as predicting how specific performance metrics impact momentum dynamics[6].

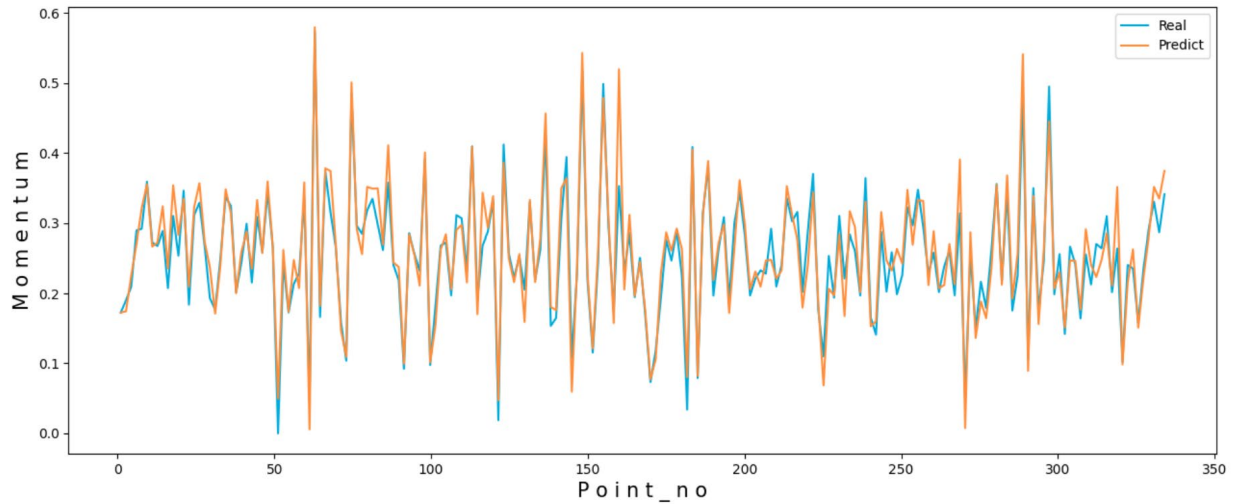


Figure 2 Real Momentum vs predict Momentum

Figure 2 shows a comparison between real momentum and LSTM model predictions. The blue line represents actual momentum, while the orange line indicates predicted values, with the horizontal axis showing match point sequence (0-350) and the vertical axis displaying momentum values (0.0-0.6). The two curves align closely, validating the model's excellent predictive performance ( $R^2=0.9501$ ), while revealing the frequency and complexity of momentum shifts in tennis matches.

#### 4. Results

The analysis of the 2023 Wimbledon final between Alcaraz and Djokovic revealed distinct playing styles, with Alcaraz leading in winners while Djokovic maintained lower unforced errors. Statistical testing confirmed that momentum patterns were not random occurrences ( $p=0.008$ ), and logistic regression validated momentum as a significant predictor of match outcomes (McFadden's  $R^2=0.42$ , accuracy=78.3%)[7]. Feature importance analysis identified unforced errors (24.7%), winners (18.3%), and break point conversions (16.5%) as the most influential factors affecting momentum.

The LSTM model demonstrated superior performance in predicting momentum changes ( $R^2=0.9501$ , accuracy=86.3%), significantly outperforming traditional methods. While the model showed good robustness against data noise and cross-gender applicability, performance varied across court surfaces, with lower accuracy on clay courts compared to hard and grass courts. The framework also demonstrated promising applicability to other racket sports like badminton and table tennis, suggesting potential for a unified momentum model across different adversarial ball sports.

#### 5. Conclusion

This study presents a novel framework for quantifying and predicting momentum in professional tennis matches using hierarchical Markov models and deep learning techniques. Our momentum metric integrates technical, psychological-tactical, and strategic factors, with statistical validation confirming momentum as a non-random phenomenon. Feature importance analysis revealed unforced errors (24.7%), winners (18.3%), and break point conversions (16.5%) as the most impactful factors on momentum, challenging conventional wisdom that aggressive play is always optimal.

Our approach has limitations, including varying performance across court surfaces and smaller sample sizes for women's matches. Strategic recommendations include prioritizing consistency during momentum-critical junctures, developing specialized tactics for break points, and

implementing structured recovery protocols following negative momentum shifts.

This methodology represents a significant advancement in quantifying the previously abstract concept of momentum in tennis. By providing objective metrics and identifying key determinants, our work bridges the gap between intuitive understanding and analytical approaches to match dynamics, establishing a foundation for sophisticated performance models that can enhance training, match strategy, and spectator engagement[8].

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